Combinations and Permutation (HKMO Classified Questions by topics)

1982 FI2.2

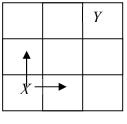
在17人之中揀選15人,共有b種方法,求b的值。

If there are b ways of choosing 15 people from 17 people, find the value of b.

1983 FI4.1

右方棋盤為一 3×3 九宮格。一隻棋子放置在 X 的位置上,每次只可向上行一格,或向右行一格。問:由 X 行到 Y,共有多少種不同的路徑?

The figure shows a board consisting of nine squares. A counter originally on square X can be moved either upwards or to the right one square at a time. By how many different routes may the counter be moved from X to Y?



1984 FG10.3

一凸 n 邊形有 14 條對角線,求 n 的值。

An n-sided convex polygon has 14 diagonals. Find the value of n.

1985 FG8.3

一凸 20 邊形有 x 條對角線。求 x 的值。

A convex 20-sided polygon has x diagonals. Find the value of x.

1988 FG6.2

一凸n邊形有35條對角綫。求n的值。

A convex n-sided polygon has 35 diagonals. Find the value of n.

1989 FG6.1

一凸 n 邊形有 20 條對角線。求 n 的值。

An n-sided convex polygon has 20 diagonals. Find the value of n.

1991 FI2.3

若一凸 n 邊形有 54 條對角綫, 求 n 的值。

If an n-sided polygon has 54 diagonals, find the value of n.

1993 HG9

一正方形的每邊被均分為四份,且以直綫連接如圖。 求非正方形的長方形數目。

Each side of a square is divided into four equal parts and straight lines are joined as shown in the figure. Find the number of rectangles which are not squares.

1994 FG6.4

從六名男士及四名女士中選出五人,組成一組。若其間共有d種選法,使男士必多於女士,求d的值。

A group of 5 people is to be selected from 6 men and 4 women. Find *d*, the number of ways that there are always more men than women.

1997 FG2.4

若將 5 個女孩排成一列, 共有 d 個不同方法。求 d 的值。

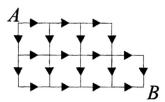
There are d different ways for arranging 5 girls in a row. Find the value of d.

1998 HG6

在圖,沿箭頭方向前進,

求 A 到 B 點的不同路綫數目。

In the figure, find the number of possible paths from point A to point B following the direction of arrow heads.



1998 FI5.3

若有c種排法把b位女孩排成一圓,求c的值。

If there are c ways of arranging 5 girls in a circle, find the value of c.

1999 HI3

已知 8 點,其中沒有任何 3 點是共綫的。求以任意 3 點作為三角形頂點的三角形的個數。

8 points are given and no three of them are collinear. Find the number of triangles formed by using any 3 of the given points as vertices.

2000 HI4

在圖一,有一個4×3的矩形蜘蛛網。若有一隻蜘 North D 蛛沿著網絲爬行。而其爬行方向衹可向東或向 北。該蜘蛛由 A 點到 C 點共有多少種可能路徑? Figure 1 represents a 4×3 rectangular spiderweb.

If a spider walks along the web from A to C and it always walks either due East or due North. Find the total number of possible paths.

2000 HI6

於一白紙上,畫有 20 條直綫。該 20 條直綫,並沒有兩條或兩條以上是平行的,也沒有三條或三條以上的直綫共點,問這 20 條直綫最多可構成多少個交點?

Twenty straight lines were drawn on a white paper. Among them, no two or more straight lines are parallel; also no three or more than three straight lines are concurrent.

What is the maximum number of intersections that these 20 lines can form?

2000 HG5

有5個分別標上A、B、C、D、E的球及5個分別標上A、B、C、D、E的 袋,每個袋放一個球。求恰好有3個球的標號與袋的標號相同的投放方法 總數。

There are 5 balls with labels A, B, C, D, E respectively and there are 5 pockets with labels A, B, C, D, E respectively. A ball is put into each pocket. In the figure, a square with area equal to 25 cm² is divided into 25 small squares with side length equal to 1 cm. If the

Find the number of ways in which exactly 3 balls have labels that match the labels on the pockets.

2000 FG3.4

在坐標平面的原點上有一點 P。假如擲出骰子的點數 n 是偶數,P 在 x 方 一個正 8 邊形共有 d 條對角綫,求 d 的值。 向右前進n;如果n是奇數,P在y方向上前進n。如果有d種不同擲法使 A regular 8-sided polygon has d diagonals, find the value of d. 得P到達點(4,4),求d的值。

P is a point located at the origin of the coordinate plane. When a dice is thrown and the number n shown is even, P moves to the right by n. If n is odd, P moves upward by n. Find the value of d, the total number of tossing sequences for P to move to the point (4, 4).

2000 FG4.4

 $A \cdot B \cdot C \cdot D \cdot E \cdot F \cdot G$ 七個人圍圓桌而坐。如果 $B \not \in G$ 都與 C 相鄰而坐 的坐法總數為d,求d的值。

A, B, C, D, E, F, G are seven people sitting around a circular table. If d is the total number of ways that B and G must sit next to C, find the value of d.

2001 HG2

把 10 個完全相同的球放入 3 個不同的盒子裏,使得沒有一個盒子是空的, find the value of X. 共有多少種放法?

In how many ways can 10 identical balls be distributed into 3 different boxes such 如圖二,兩個邊長為 1 cm 的正方體組成一個 that no box is to be empty?

2001 FI4.2

若一正 Q 邊形有 35 條對角綫, 求 Q 的值。

If a regular *Q*-sided polygon has 35 diagonals, find the value of *Q*.

2003 HI5

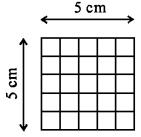
課室內有 n 個人,若每個人恰好跟其他人各握手一次,則共有 28 次握手, 求 n 的值。

There are *n* persons in the classroom. If each person in the classroom shakes hands exactly once with each other person in the classroom and there are altogether 28 handshakes. Find the value of n.

2003 HI8

圖中,一個面積為 25 cm² 的正方形被分成 25 個邊 長為 1 cm 的小正方形。若圖中共有 K 個不同的正方 形, \bar{x} K 的值。

total number of different squares in the figure is K, find the value of K.



2005 FI1.4

2006 HI6

已知 $w \cdot x \cdot v$ 和 z 是正整數且滿足方程 w + x + v + z = 12。若方程有 W組不同的正整數解,求W的值。

Given that w, x, y and z are positive integers which satisfy the equation w + x + y + z = 12. If there are W sets of different positive integral solutions of the equation, find the value of W.

2007 HI3

在4本英文書、6本中文書及9本日文書中任取兩本。已知這兩本書是相同 語言的。若有 X 個不同的選擇, 求 X 的值。

Among 4 English books, 6 Chinese books and 9 Japanese books, two books are selected. It is found that they are of the same language. If there are X such choices,

2007 HG5

1 cm×1 cm×2 cm 的長方體。一隻螞蟻沿著長方體 爬行,其爬行路綫須為正方體的棱。牠從頂點 A 出 發,以每分鐘爬行 1 cm 的速度,於 4 分鐘後到達 頂點 B。若螞蟻可行路綫數目共有 S 個, 求 S的值。

In Figure 2, a 1 cm \times 1cm \times 2 cm rectangular box is made by two cubes with side length 1 cm. An ant is

climbing along the box in a way that it must stay on the edges of the cubes through out the climbing. Starting from vertex A and climbing with a speed of 1 cm per minutes, it reaches vertex B after 4 minutes. If the total number of possible paths taken by the ant is S, find the value of S.

2008 FG3.4

當從標明了1至30的30個號碼球中選出4個,而選出的球均不放回重選從1、2、4、6、7中選三個數字組成三位數。 時,能得r個組合,求r的值。

When choosing, without replacement, 4 out of 30 labelled balls that are marked Choose three digits from 1, 2, 4, 6, 7 to construct three-digit numbers. Of these from 1 to 30, there are r combinations. Find the value of r.

2010 HI1

把 8 個完全相同的球放入三個不同的盒中,使得每個盒內至少有球一個, 問共有多少個不同的分配方法?

In how many possible ways can 8 identical balls be distributed to 3 distinct boxes 2) so that every box contains at least one ball?

2010 FI2.3

在一個 5×5 的棋盤上任意選取兩個不在同一橫行上方格。

若c為選取的兩個不同方格的組合數目,求c的值。

In a 5×5 checkerboard, two squares not lying in the same row are randomly chosen. If c is the number of combinations of different pairs of squares chosen, find the value of c.

2011 FI1.4

若S為安排8個人圍成圓形的數目,求S的值。

If S is the number of ways to arrange 8 persons in a circle, find the value of S. 2012 HI2

已知 $a \cdot b$ 及 c 為正偶數,且滿足方程 a+b+c=2012。問該方程共有多 少個解?

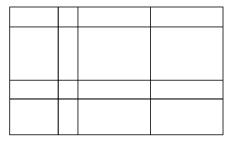
Given that a, b and c are positive even integers which satisfy the equation a + b + c = 2012. How many solutions does the equation have?

2013 FI1.1

圖中共有 a 個長方形, 求 a 的值。

The figure has a rectangles,

find the value of a.



2013 FG1.3

這些三位數有多少個能被3整除?

three-digit numbers, how many of them are divisible by 3?

2013 FG2.2

三男 $B_1 \, \cdot \, B_2 \, \cdot \, B_3$ 和三女 $G_1 \, \cdot \, G_2 \, \cdot \, G_3$ 就坐一排座位,並滿足以下兩個條件:

- 一男不會坐在另一男旁邊及一女不會坐在另一女旁邊
- B_1 必須坐在 G_1 旁邊

若 S 是這樣就坐的排列數量,求S的值。

Three boys B_1 , B_2 , B_3 and three girls G_1 , G_2 , G_3 are to be seated in a row according to the following rules:

- A boy will not sit next to another boy and a girl will not sit next to another girl,
- Boy B_1 must sit next to girl G_1

If s is the number of different such seating arrangements, find the value of s.

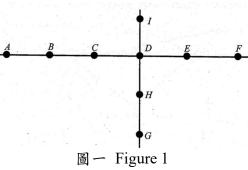
2015 HI1

在1至2015之間(包括1及2015在內)有多少對相異整數的積是5的倍數? How many pairs of distinct integers between 1 and 2015 inclusively have their products as multiple of 5?

2017 HG2

如圖一所示,點 $A \cdot B \cdot C \cdot D \cdot E$ 及 F均在一直幾上。點 $G \cdot H \cdot D \otimes I$ 在 另一直幾上。揀選三點,可形成多少一 個三角形?

As shown in Figure 1, points A, B, C, D, E and F lie on the same straight line, and G, H, D and I lie on another straight line. How many triangles can be made by connecting any three points?



2017 FG2.2

立方體的任意兩個頂點可相連成一線段。若 B 為最多所能夠相連成的直線 的數量, 求 B 的值。

Any two vertices in a cube can form a line segment. If B is the greatest number of line segments thus formed, determine the value of B.

2018 HG8

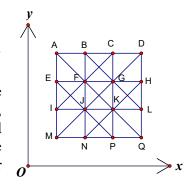
已知 $a \cdot b \cdot c \cdot d \cdot e \cdot f \cdot g$ 及 h 為正整數,使得 a > b > c > d > e > f > g > h 及 a + h = b + g = c + f = d + e = 35,問有多少組可行答案 $\{a, b, c, d, e, f, g, h\}$ 存在?

Given that a, b, c, d, e, f, g and h are positive integers such that a > b > c > d > e > f > g > h and a + h = b + g = c + f = d + e = 35. How many possible solution sets of $\{a, b, c, d, e, f, g, h\}$ exist?

2019 HI6

在圖三中,直角座標平面上一個正方形的四個頂點的座標分別為 (1,1)、(1,4)、(4,1)及(4,4)。若在該正方形中(包括邊界)選擇任何三個座標均為整數的點,問可組成多少個三角形?

In Figure 3, the vertices of a square in the rectangular coordinate plane are (1, 1), (1, 4), (4, 1) and (4, 4). How many triangles can be formed by selecting any three points in the square (including the boundaries) with integer coordinates?



2023 HG4

排列 5 個不同的單數及 5 個不同的雙數在同一行使得任意兩個相鄰數的積 必為雙數。求所有排列的可能性數目。

Five distinct odd numbers and five distinct even numbers are arranged in a row such that the product of any two consecutive numbers is always even.

Find the number of all possible arrangements.

2023 FI2.4

在 x-y 座標平面上,每一步移動都包含 x 座標和 y 座標分別增加(或減少)1 個單位(即對角幾移動)。若 δ 是由 (0,0) 開始行走 12 步後到達 (-4,-4) 的方法的數目,求 δ 的值。

On the *x-y* coordinate plane, a move consists of independently increasing (or decreasing) *x*-coordinate and *y*-coordinate by 1 (i.e. moving diagonally).

If δ is the number of ways to start from (0, 0), make 12 moves and end at (-4, -4), find the value of δ .

2024 FG1.3

有多少個 5 位數包含最少 1 個「1」和最少 1 個「3」?

How many 5-digit numbers contain at least one "1" and at least one "3"?

Answers

1982 FI2.2 1983 FI4.1 1984 FG10.3 1985 FG8.3 1988 FG6.2 136 6 7 170 10 1989 FG6.1 1991 FI2.3 1993 FG9 1994 FG6.4 1997 FG2.4 8 12 70 186 120 1998 HG6 1998 FI5.3 1999 HI3 2000 HI4 2000 HI6 14 24 56 35 190 2000 HG5 2000 FG3.4 2000 FG4.4 2001 HG2 2001 FI4.2 10 38 48 36 10 2003 HI5 2003 HI8 2005 FI1.4 2006 HI5 2007 HI3 8 55 20 165 57 2007 HG5 2008 FG3.4 2010 HI1 2010 FI2.3 2011 FI1.4 12 27405 21 200 5040 2012 HI2 2013 FI1.1 2013 FG1.3 2013 FG2.2 2015 HI1 504510 100 24 40 730639 2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400	Answers				
1989 FG6.1 1991 FI2.3 1993 FG9 1994 FG6.4 1997 FG2.4 8 12 70 186 120 1998 HG6 1998 FI5.3 1999 HI3 2000 HI4 2000 HI6 14 24 56 35 190 2000 HG5 2000 FG3.4 2000 FG4.4 2001 HG2 2001 FI4.2 10 38 48 36 10 2003 HI5 2003 HI8 2005 FI1.4 2006 HI5 2007 HI3 8 55 20 165 57 2007 HG5 2008 FG3.4 2010 HI1 2010 FI2.3 2011 FI1.4 12 27405 21 200 5040 2012 HI2 2013 FI1.1 2013 FG1.3 2013 FG2.2 2015 HI1 504510 100 24 40 730639 2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400 2023 FI2.4 2024 FG1.3 2024 FG1.3 2024 FG1	1982 FI2.2	1983 FI4.1	1984 FG10.3	1985 FG8.3	1988 FG6.2
8 12 70 186 120 1998 HG6 1998 FI5.3 1999 HI3 2000 HI4 2000 HI6 14 24 56 35 190 2000 HG5 2000 FG3.4 2000 FG4.4 2001 HG2 2001 FI4.2 10 38 48 36 10 2003 HI5 2003 HI8 2005 FI1.4 2006 HI5 2007 HI3 8 55 20 165 57 2007 HG5 2008 FG3.4 2010 HI1 2010 FI2.3 2011 FI1.4 12 27405 21 200 5040 2012 HI2 2013 FI1.1 2013 FG1.3 2013 FG2.2 2015 HI1 504510 100 24 40 730639 2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400 2023 FI2.4 2024 FG1.3 2024 FG1.3 2024 FG1.3	136	6	7	170	10
1998 HG6 1998 FI5.3 1999 HI3 2000 HI4 2000 HI6 14 24 56 35 190 2000 HG5 2000 FG3.4 2000 FG4.4 2001 HG2 2001 FI4.2 10 38 48 36 10 2003 HI5 2003 HI8 2005 FI1.4 2006 HI5 2007 HI3 8 55 20 165 57 2007 HG5 2008 FG3.4 2010 HI1 2010 FI2.3 2011 FI1.4 12 27405 21 200 5040 2012 HI2 2013 FI1.1 2013 FG1.3 2013 FG2.2 2015 HI1 504510 100 24 40 730639 2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400 2023 FI2.4 2024 FG1.3 2024 FG1.3 2024 FG1.3	1989 FG6.1	1991 FI2.3	1993 FG9	1994 FG6.4	1997 FG2.4
14 24 56 35 190 2000 HG5 2000 FG3.4 2000 FG4.4 2001 HG2 2001 FI4.2 10 38 48 36 10 2003 HI5 2003 HI8 2005 FI1.4 2006 HI5 2007 HI3 8 55 20 165 57 2007 HG5 2008 FG3.4 2010 HI1 2010 FI2.3 2011 FI1.4 12 27405 21 200 5040 2012 HI2 2013 FI1.1 2013 FG1.3 2013 FG2.2 2015 HI1 504510 100 24 40 730639 2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400 2023 FI2.4 2024 FG1.3 2024 FG1.3 86400	8	12	70	186	120
2000 HG5 2000 FG3.4 2000 FG4.4 2001 HG2 2001 FI4.2 10 38 48 36 10 2003 HI5 2003 HI8 2005 FI1.4 2006 HI5 2007 HI3 8 55 20 165 57 2007 HG5 2008 FG3.4 2010 HI1 2010 FI2.3 2011 FI1.4 12 27405 21 200 5040 2012 HI2 2013 FI1.1 2013 FG1.3 2013 FG2.2 2015 HI1 504510 100 24 40 730639 2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400 2023 FI2.4 2024 FG1.3 2024 FG1.3 2024 FG1.3	1998 HG6	1998 FI5.3	1999 HI3	2000 HI4	2000 HI6
10 38 48 36 10 2003 HI5 2003 HI8 2005 FI1.4 2006 HI5 2007 HI3 8 55 20 165 57 2007 HG5 2008 FG3.4 2010 HI1 2010 FI2.3 2011 FI1.4 12 27405 21 200 5040 2012 HI2 2013 FI1.1 2013 FG1.3 2013 FG2.2 2015 HI1 504510 100 24 40 730639 2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400 2023 FI2.4 2024 FG1.3 86400	14	24	56	35	190
2003 HI5 2003 HI8 2005 FI1.4 2006 HI5 2007 HI3 8 55 20 165 57 2007 HG5 2008 FG3.4 2010 HI1 2010 FI2.3 2011 FI1.4 12 27405 21 200 5040 2012 HI2 2013 FI1.1 2013 FG1.3 2013 FG2.2 2015 HI1 504510 100 24 40 730639 2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400 2023 FI2.4 2024 FG1.3 2017 FG2.2 2017 FG2.2	2000 HG5	2000 FG3.4	2000 FG4.4	2001 HG2	2001 FI4.2
8 55 20 165 57 2007 HG5 2008 FG3.4 2010 HI1 2010 FI2.3 2011 FI1.4 12 27405 21 200 5040 2012 HI2 2013 FI1.1 2013 FG1.3 2013 FG2.2 2015 HI1 504510 100 24 40 730639 2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400 2023 FI2.4 2024 FG1.3 86400	10	38	48	36	10
2007 HG5 2008 FG3.4 2010 HI1 2010 FI2.3 2011 FI1.4 12 27405 21 200 5040 2012 HI2 2013 FI1.1 2013 FG1.3 2013 FG2.2 2015 HI1 504510 100 24 40 730639 2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400 2023 FI2.4 2024 FG1.3 2024 FG1.3 2024 FG1.3	2003 HI5	2003 HI8	2005 FI1.4	2006 HI5	2007 HI3
12 27405 21 200 5040 2012 HI2 2013 FI1.1 2013 FG1.3 2013 FG2.2 2015 HI1 504510 100 24 40 730639 2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400 2023 FI2.4 2024 FG1.3 86400 86400	8	55	20	165	57
2012 HI2 2013 FI1.1 2013 FG1.3 2013 FG2.2 2015 HI1 504510 100 24 40 730639 2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400 2023 FI2.4 2024 FG1.3 86400	2007 HG5	2008 FG3.4	2010 HI1	2010 FI2.3	2011 FI1.4
504510 100 24 40 730639 2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400 2023 FI2.4 2024 FG1.3 86400 86400	12	27405	21	200	5040
2017 HG2 2017 FG2.2 2018 HG8 2019 HI6 2023 HG4 60 28 2380 516 86400 2023 FI2.4 2024 FG1.3 300 <	2012 HI2	2013 FI1.1	2013 FG1.3	2013 FG2.2	2015 HI1
60 28 2380 516 86400 2023 FI2.4 2024 FG1.3	504510	100	24	40	730639
2023 FI2.4 2024 FG1.3	2017 HG2	2017 FG2.2	2018 HG8	2019 HI6	2023 HG4
	60	28	2380	516	86400
495 13696	2023 FI2.4	2024 FG1.3			
15070	495	13696			