Mensuration (HKMO Classified Questions by topics)

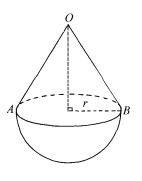
1982 FG7.1

右圖顯示一圓錐體及一半球體。OB=12 cm, r=10 cm,以 π 表示該立體的表面面積。

The figure shows a cone and a hemisphere.

OB = 12 cm, r = 10 cm.

Express the surface area of the solid in terms of π .



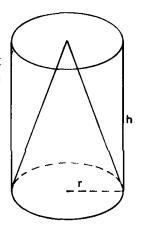
1982 FG7.2

以 π 表示上圖立體的體積。

What is the volume of the hemisphere shown in the above figure ? Give your answer in terms of π .

1982 FG7.3

右圖顯示一圓錐體放置在一個半徑相等(r)、高度相同(h)的圓柱體內,以r及h表示兩者之間的空間的體積。 In the figure, a right circular cone stands inside a right cylinder of same base radius r and height h. Express the volume of the space between them in terms of r and h.



1982 FG7.4

求圚柱體與圚錐體體積之比。

Find the ratio of the volume of the cylinder to that of the cone.

1984 FI3.2

若 $b \text{ cm}^2$ 為一邊長 1 cm 的立方體之總表面積,求b的值。

If $b \text{ cm}^2$ is the total surface area of a cube of side 1 cm, find the value of b.

1984 FG9.2

一長方體之長、闊、高依次為 2×3 及 4×6 若其總面積為 $A \times 6$ 的值。 The length, width and height of a rectangular block are 2,3 and 4 respectively. Its total surface area is A, find the value of A.

1985 FSI.2

若一邊長3 cm之正方體之總表面積為 $b \text{ cm}^2$,求b的值。

If $b \text{ cm}^2$ is the total surface area of a cube of side 3 cm, find the value of b.

1986 FI2.2

若一圓柱體之高增加一倍,且新半徑為原來之 4 倍,則新體積為原來之 k 倍,求 k 的值。

If the height of a cylinder is doubled and the new radius is 4 times the original, then the new volume is k times the original. Find the value of k.

1986 FI5.4

一角錐體之底為三角形,其邊長分別為 3 cm,4 cm 及 5 cm。若該角錐體之高及體積依次為 q cm 及 12 cm^3 ,求 q 的值。

The base of a pyramid is a triangle with sides 3 cm, 4 cm and 5 cm. If the height and volume of the pyramid are q cm and 12 cm³ respectively, find the value of q.

1987 FI2.1

某球體之半徑為 r, 體積為 36π, 求 r 的值。

The volume of a sphere with radius r is 36π , find the value of r.

1989 FG9.2

一長方體闊 y cm,長 6 cm,高 5 cm。它的表面積是 126 cm²,求 y 的值。 A cuboid is y cm wide, 6 cm long and 5 cm high. Its surface area is 126 cm². Find the value of y.

1991 FI3.2

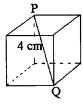
一個邊長 7 cm 之正方體在全部面上都塗上紅色後,再被分割為邊長 1 cm 之正方體。若所有面都未有被塗上顏色之正方體數目為 b,求 b 的值。

A cube with edge 7 cm long is painted red on all faces. It is then cut into cubes with edge 1 cm long. If the number of cubes with all the faces not painted is b, find the value of b.

1992 HI14

在圖中,PQ 為一正方體的對角綫。若 PQ=4 cm,且這正方體的總表面面積為 x cm²,求 x 的值。

In the figure, PQ is a diagonal of the cube. If PQ = 4 cm and the total surface area of the cube is $x \text{ cm}^2$, find the value of x.



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1992 FG8.4

某三角錐體之底為一邊長6cm之等邊三角形。

若該三角錐體之高為 $\sqrt{27}$ cm,且其體積為d cm³,求d 的值。

The base of a triangular pyramid is an equilateral triangle of side 6 cm.

If the height of the pyramid is $\sqrt{27}$ cm, and its volume is d cm³. find the value of d.

1993 HI5

一長方形盒子的三塊不同面的面積分別為 120、72 和 60。求該盒子的體積。 The areas of three different faces of a rectangular box are 120, 72 and 60 respectively. Find its volume.

1994 HG2

一實心正方體邊長 9 cm。現將這正方體表面全部塗上顏色,然後分割為 27 個 邊長為3cm 的全等小正方體。求這些小正方體沒有塗上顏色的面的總面積。 A solid cube with edges of length 9 cm is painted completely on the outside. It is 在圖中,圓管的長為20及直徑為6,內有兩個圓錐體 A 和 B。A 及 B 的體 then cut into 27 congruent little cubes with edges 3 cm.

Find the total area of the unpainted faces of these cubes.

1994 FI5.2

若 B 條內直徑為 1 厘米的圓形水管的輸水量與一內直徑為 6 厘米的圓形水 管相等, 求 B 的值。

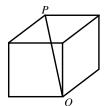
If B circular pipes each with an internal diameter of 1 cm carry the same amount of water as a pipe with an internal diameter 6 cm, find the value of B.

1995 FI5.2

如圖示,PQ是正方體的一條對角綫,且PQ=1。 若b為此正方體的總表面積,求b的值。

In the figure, PQ is a diagonal of the cube and PQ = 1.

Find the value of b, if b is the total surface area of the cube.



1996 FI1.3

圖中為一圓柱體和半球體組成的無蓋空心物體。半球體和圓 柱體的半徑均為 1 cm。若這物體的長度為 1 cm,且表面面 積為 $c\pi$ cm², 求 c 的值。

The figure shows an open cylindrical tube (radius = 1 cm) with $\frac{1 \text{ cm}}{1 \text{ cm}}$ a hemispherical bottom of radius 1 cm. The height of the tube is

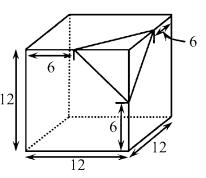
18 cm and the external surface area of the tube is $c\pi$ cm².

Find the value of c.

1997 FI2.2

如圖所示,從邊長為 12 cm 的正立方體的一 角割出一個三角錐體。若三角錐體的體積為 $b \text{ cm}^3$, 求b的值。

A triangular pyramid is cut from a corner of a 1 cube with side length 12 cm as the figure shown. If the volume of the pyramid is $b \text{ cm}^3$, find the value of b.



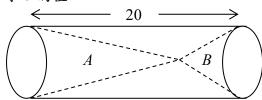
1997 FI5.1

一直徑為a的半球體的體積為 18π cm³,求a的值。

The volume of a hemisphere with diameter a cm is 18π cm³, find the value of a. 2000 FG3.2

積比例為3:1。如果b是B的高度,求b的值。

In the figure, A and B are two cones inside a cylindrical tube with length of 20 and diameter of 6. If 6 the volumes of A and B are in the $\sqrt{}$ ratio 3:1 and b is the height of the cone B, find the value of b.

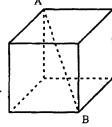


2003 HI7

在圖中,正方體的對角綫 AB 的長度是 $\sqrt{12}$ cm。若該正

方體的體積是 $M \, \text{cm}^3$,求M的值。

In the figure, AB is a diagonal of the cube and $AB = \sqrt{12}$ cm. If the volume of the cube is $M \text{ cm}^3$, find the value of M.



2005 HG6

若一正八面體的邊長為 1 cm ,其體積為 $f \text{ cm}^3$,求 f 的值。

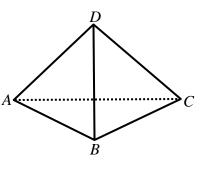
Suppose the side of a regular octahedron is equal to 1 cm and the volume is equal to $f \text{ cm}^3$, find the value of f.

2008 HG3

如圖,正四面體 ABCD 的邊長為 2 cm。若該

正四面體的體積是 \sqrt{R} cm³, 求 R 的值。

In the figure, ABCD is a regular tetrahedron with side length of 2 cm. If the volume of the tetrahedron is \sqrt{R} cm³, find the value of R.



2010 FI1.1

把三個體積分別為1、8、27的正立方體,以面同貼面的方法黏合起來。 若 a 為所得的多面體的最小總表面積,求 a 的值。

Three cubes with volumes 1, 8, 27 are glued together at their faces. If a is the smallest possible surface area of the resulting polyhedron, find the value of a.

2013 FI2.2

一正方體的表面積是 $b \text{ cm}^2$ 。若它每一條邊的長度增加 3 cm,它的體積隨之增加 $(2b-3) \text{ cm}^3$,求 b 的值。

The surface area of a cube is $b \text{ cm}^2$. If the length of each side is increased by 3 cm, its volume is increased by $(2b-3) \text{ cm}^3$, find the value of b.

2023 FG4.3

如果正四面體的邊長是1,求該正四面體的體積。 If the length of one side of a regular tetrahedron is 1, find the volume of such tetrahedron.

Answers

1982 FG7.1 320π cm ²	$\frac{1982 \text{ FG7.2}}{2000\pi} \text{ cm}^3$	$\frac{1982 \text{ FG7.3}}{\frac{2}{3}\pi r^2 h}$	1982 FG7.4 3 : 1	1984 FI3.2 6
1984 FG9.2	1985 FSI.2	1986 FI2.2	1986 FI5.4	1987 FI2.1
52	54	32	6	3
1989 FG9.2	1991 FI3.2	1992 HI14	1992 FG8.4	1993 HI5
3	125	32	27	720
1994 HG2	1994 FI5.2	1995 FI5.2	1996 FI1.3	1997 FI2.2
972 cm ²	36	2	36	36
1997 FI5.1	2000 FG3.2	2003 HI7	$\frac{2005 \text{ HG6}}{\frac{\sqrt{2}}{3}}$	2008 HG3
6	5	8		8/9
2010 FI1.1 72	2013 FI2.2 600	2023 FG4.3 $\frac{\sqrt{2}}{12}$		