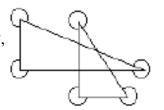
Hong Kong Mathematics Olympiad (1982-83) Event 1 (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 如圖,所有有記號的角的總和是 a° ,求 a 的值。 In the following figure, the sum of the marked angles is a° , find the value of a.





(ii) 一正 b-邊形的內角和是 a° 。求 b 的值。

The sum of the interior angles of a regular b-sided polygon is a° . Find the value of b.

b =

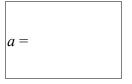
(iii) 求 c 的值,若 $2^b = c^4$ 及 c > 0。 Find the value of c, if $2^b = c^4$ and c > 0.

(iv) 若 $\frac{b}{c} = k$ 及 c: d = k: 100,求 d 的值。 Find the value of d, if $\frac{b}{c} = k$ and c: d = k: 100.

d =

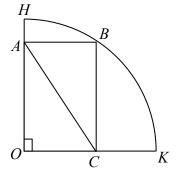
Hong Kong Mathematics Olympiad (1982-83) Event 3 (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。



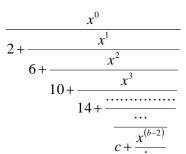
(ii) 如圖, OH = OK = 10 及 OABC 為一個長方形。 AC = b, 問 b 為何值?

In the diagram shown, OH = OK = a units and OABC is a rectangle. AC = b units. What is the value of b?



b =

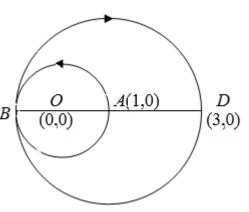
(iii) 依下圖之分數,當計算至分子是 x^8 時,c 為何值? In the expression shown, what is c when it is expanded to the term with $x^{(b-2)}$ as the numerator?



c =

(iv) 如圖,一兔子花了 c 分鐘經半圓跑道由 A 去到 B。以相同速度,牠花了 d 分鐘經半圓 跑道由 $A \to B \to D$ 。問 d 為何值?

As shown a rabbit spends c minutes in travelling from A to B along half circle. With the same speed, it spends d minutes in B travelling from $A \rightarrow B \rightarrow D$ along half circles. What is the value of d?



d =

FOR OFFICIAL USE

Score for accuracy

× Mult. factor for speed



Team No.



+ Bonus score



Time



Total score



Min.

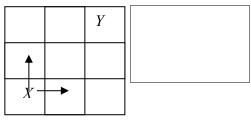
Hong Kong Mathematics Olympiad (1982-83) Event 4 (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 右方棋盤為 -3×3 九宮格。-隻棋子放置在 X 的位置上,每次只可向上行一格,或向右行一格。

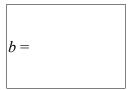
問:由X行到Y,共有多少種不同的路徑?

The figure shows a board consisting of nine squares. A counter originally on square X can be moved either upwards or to the right one square at a time. By how many different routes may the counter be moved from X to Y?



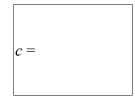
(ii) 已知 $\sqrt{2a} = -b \tan \frac{\pi}{3}$ 。求 b 的值。

Given $\sqrt{2a} = -b \tan \frac{\pi}{3}$. Find the value of b.



(iii) 已知 $p*q = \frac{p-q}{p}$, 求 c 的值,若 c = (a+b)*(b-a)。

Given that $p * q = \frac{p-q}{p}$, find the value of c if c = (a+b)*(b-a).



(iv) 把一 c cm 的鐵綫屈曲成一半徑為 1 cm 的扇形。問扇形的圓心角為何? A wire of c cm is bent to form a sector of radius 1 cm. What is the angle of the sector in degrees (correct to the nearest degree)?

angle =

<u>FOR</u>	<u>OFFICIAL</u>	USE

Score for accuracy

Mult. factor for speed



Team No.

+ Bonus score

Time



Sec.

Total score

Hong Kong Mathematics Olympiad (1982-83) Event 5 (Individual)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 若 $a(x+1) \equiv x^3 + 3x^2 + 3x + 1$,以 x 表示 a。 If $a(x+1) \equiv x^3 + 3x^2 + 3x + 1$, express a in terms of x.

a =

(ii) $\ddot{a} = a - 1 = 0$,則 x 的解為 0 或 b,求 b 的值。 If a - 1 = 0, then the value of x is 0 or b, what is the value of b?

b =

(iii) 若 $pc^4 = 32$, $pc = b^2$ 及 c 為正數, c 的值為何? If $pc^4 = 32$, $pc = b^2$ and c is positive, what is the value of c?

c =

(iv) P 為一運算子使得 $P(A \cdot B) = P(A) + P(B)$ 。 P(A) = y 的意思是 $A = 10^y$ 。若 $d = A \cdot B$,P(A) = 1 及 P(B) = c,求 d 的值。 P is an operation such that $P(A \cdot B) = P(A) + P(B)$. P(A) = y means $A = 10^y$. If $d = A \cdot B$, P(A) = 1 and P(B) = c, find the value of d.

d =

FOR OFFICIAL USE

Hong Kong Mathematics Olympiad (1982-83) Event 6 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 右表顯示二元運算子*定義於 P、Q、R、S 時的結果。假設 a 為 P 的反元素。求 a 的值。 The table shows the results of the operation * on P, Q, R, S taken two at a time. Let a be the inverse of P. Find the value of a.

* on	P	Q	R	S	
OII	Q	R	S	P	
f a .	R	S	P	O	

<i>a</i> =		

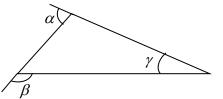
P

Q

S

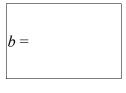
(ii) α 與 β 的平均值是 105° , α 、 β 與 γ 的平均值是 b° 。求b的值。

The average of α and β is 105°, the average of α , β and γ is b°. Find the value of b.



0

R



(iii) 兩數之和為 10,其乘積為 20。若該兩倒數之和為 c,求 c 的值。 The sum of two numbers is 10, their product is 20. The sum of their reciprocal is c. What c= is the value of c?

That c =

(iv) 已知 $\sqrt{90}$ = 9.49 (準至雨位小數) 若 $d < 7\sqrt{0.9} < d+1$, 其中 d 為整數,求 d 的值。 It is given that $\sqrt{90}$ = 9.49, to 2 decimal places. If $d < 7\sqrt{0.9} < d+1$, where d is an integer, what is the value of d?

d =

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Score for accuracy

Mult. factor for speed

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Team No.

Time

Total score

Bonus

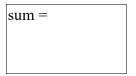
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Hong Kong Mathematics Olympiad (1982-83) Event 7 (Group)

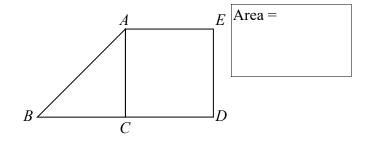
Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 求 3+6+9+...+45 的值。 Find the value of 3+6+9+...+45.



(ii) 圖中,ACDE 為一正方形,AC = BC 及 $\angle ACB = 90^{\circ}$ 。若 ACDE 的面積為 $10~\rm{cm}^2$,求 ΔABC 的面積。

In the figure shown, ACDE is a square and AC = BC, $\angle ACB = 90^{\circ}$. Find the area of ΔABC if the area of ACDE is $10~\rm{cm}^2$.



(iii) 若 $a + \frac{1}{a} = 3$, 求 $a^3 + \frac{1}{a^3}$ 的值。

Given that $a + \frac{1}{a} = 3$. Evaluate $a^3 + \frac{1}{a^3}$.



(iv) 已知 $\sum_{y=1}^{n} \frac{1}{y} = \frac{1}{1} + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n}$ 。 求 $\sum_{y=3}^{10} \frac{1}{y-2} - \sum_{y=3}^{10} \frac{1}{y-1}$ 的值。(答案以份數表示。) Given that $\sum_{y=1}^{n} \frac{1}{y} = \frac{1}{1} + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n}$.

Find the value of $\sum_{y=3}^{10} \frac{1}{y-2} - \sum_{y=3}^{10} \frac{1}{y-1}$. (Express your answer in fraction.)

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Score for accuracy

Mult. factor for speed



Team No.

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Bonus

Time

Total score

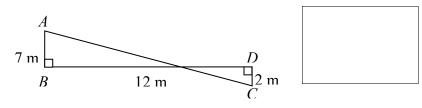
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Hong Kong Mathematics Olympiad (1982-83) Event 8 (Group)

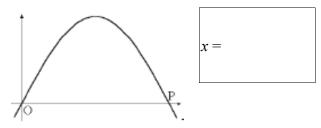
Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) 如圖,彼得站 A 點而約翰站在 C 點,BD 的距離 12 m。問彼得和約翰之間的最短距離為何?
Peter is standing at A and John is at C.
The distance between B and D is 12 m.
What is the shortest distance between

John and Peter?



(ii) 右圖顯示 $y = \sin 3x^{\circ}$ 的圖像,求 P 點的 x 座標。 The following figure shows a part of the graph $y = \sin 3x^{\circ}$. What is the x-coordinate of P?



(iii) 若 $f(x) = x^2$,以 x 表示 f(x) - f(x-1)。 If $f(x) = x^2$, then express f(x) - f(x-1) in terms of x.



(iv) 若果 $mnp \cdot nmp \cdot mmp$ 及 nnp 為十進制數字,其位值是由 $m \cdot n$ 及 p 組成,且 mnp - nmp = 180 及 mmp - nnp = d。求 d 的值。



If mnp, nmp, mmp and nnp are numbers in base 10 composed of the digits m, n and p, such that: mnp - nmp = 180 and mmp - nnp = d. Find the value of d.

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			+	Bonus score			Time		
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Total score

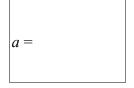
Sec.

Min.

Hong Kong Mathematics Olympiad (1982-83) Event 9 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) If $\sin \theta = \frac{3}{5}$, $a = \sqrt{\tan^2 \theta + 1}$, find the value of a.



考慮以下步驟,用以證明 $\frac{1}{8} > \frac{1}{4}$ 。 (ii)

step

Examine the following proof carefully: To prove $\frac{1}{Q} > \frac{1}{4}$.

步驟 Stens

<u>ツ</u> ッル	<u>steps</u>	
1	3 > 2	3 > 2
2	雨邊乘以 $\log\left(\frac{1}{2}\right)$,	Multiply both sides by $\log\left(\frac{1}{2}\right)$,
2	使得 $3\log\left(\frac{1}{2}\right) > 2\log\left(\frac{1}{2}\right)$	then $3 \log \left(\frac{1}{2}\right) > 2 \log \left(\frac{1}{2}\right)$
3	$\log\left(\frac{1}{2}\right)^3 > \log\left(\frac{1}{2}\right)^2$	$\log\left(\frac{1}{2}\right)^3 > \log\left(\frac{1}{2}\right)^2$
4	$\left(\frac{1}{2}\right)^3 > \left(\frac{1}{2}\right)^2$	$\left(\frac{1}{2}\right)^3 > \left(\frac{1}{2}\right)^2$

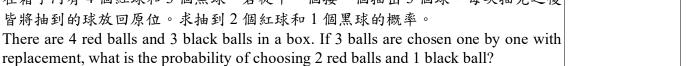
$$\therefore \frac{1}{8} > \frac{1}{4}$$

Which step is incorrect? 以上哪一步是錯的?

(iii) 若兩直幾 2y + x + 3 = 0 及 3y + cx + 2 = 0 互相垂直,求 c 的值。 If the lines 2y + x + 3 = 0 and 3y + cx + 2 = 0 are perpendicular, find the value of c.



(iv) 在箱子內有 4 個紅球和 3 個黑球。若從中一個接一個抽出 3 個球,每次抽完之後 皆將抽到的球放回原位。求抽到2個紅球和1個黑球的概率。



FOR OFFICIAL USE

Score for Mult. factor for Team No. = speed accuracy Bonus Time score Min. Total score Sec.

Hong Kong Mathematics Olympiad (1982-83) Event 10 (Group)

Unless otherwise stated, all answers should be expressed in numerals in their simplest form. 除非特別聲明,答案須用數字表達,並化至最簡。

(i) $1^2 - 1 = 0 \times 2$ $2^2 - 1 = 1 \times 3$ $3^2 - 1 = 2 \times 4$

- $1^2 1 = 0 \times 2$ $2^2 - 1 = 1 \times 3$
- $3^2 1 = 2 \times 4$

 $4^2 - 1 = 3 \times 5$

A =

......

 $4^2 - 1 = 3 \times 5$

$$A^2 - 1 = 3577 \times 3579$$

若 $A > 0$, 求 A 的值。

......

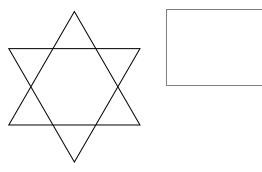
$$A^2 - 1 = 3577 \times 3579$$

If A > 0, find the value of A.

(ii) 一正 N-邊形的邊向外延長形成一個"星形"。如果 該星形的每一隻角均為 108° , 求 N 的值。(例如, 由正6邊形形成的6角星如右圖所示。)

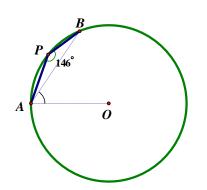
The sides of an N-sided regular polygon are produced to form a "star". If the angle at each point of that "star" is 108° , find the value of N.

(For example, the "star" of a six-sided polygon is given as shown in the diagram.)



6-sided regular polygon.

(iii) $A \cdot P \otimes B$ 三點均在圓周上,圓心為O。 若 $\angle APB = 146^{\circ}$, 求 $\angle OAB$ 的值。 A, P, B are three points on a circle with centre O. If $\angle APB = 146^{\circ}$, find the value of $\angle OAB$.



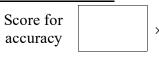
 $\angle OAB =$

(iv) 一兩位數 X 的個位與十位相乘等於 24,若將個位與十位對掉,新的兩位數 比原來的兩位數大了 18, 求 X的值。

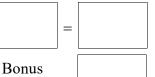
A number X consists of 2 digits whose product is 24. By reversing the digits, the new number formed is 18 greater than the original one. What is the value of X?



FOR OFFICIAL USE



Mult. factor for speed



Team No.



Total score

score



Time



Min.