

1. Find the unit vector in the direction of $-\mathbf{i} + 2\mathbf{j}$.	2. Find the unit vector in the direction of $3\mathbf{i} - 4\mathbf{j} + 12\mathbf{k}$.
Ans. $-\frac{1}{\sqrt{5}}\mathbf{i} + \frac{2}{\sqrt{5}}\mathbf{j}$	Ans. $\frac{3}{13}\mathbf{i} - \frac{4}{13}\mathbf{j} + \frac{12}{13}\mathbf{k}$
3. Find the vector with length = 3 and in the same direction as $-\mathbf{i} + 2\mathbf{j}$.	4. Find the vector with length = 13 which is parallel to $3\mathbf{i} - 4\mathbf{j} + 12\mathbf{k}$.
Ans. $-\frac{3}{\sqrt{5}}\mathbf{i} + \frac{6}{\sqrt{5}}\mathbf{j}$	Ans. $\pm(3\mathbf{i} - 4\mathbf{j} + 12\mathbf{k})$
5. Let $\mathbf{a} = 3\mathbf{i} + 4\mathbf{j}$, $\mathbf{b} = -\mathbf{i} + 2\mathbf{j}$. Find $\mathbf{a} \cdot \mathbf{b}$.	6. Let $\mathbf{a} = 3\mathbf{i} - 4\mathbf{j} + 12\mathbf{k}$, $\mathbf{b} = 2\mathbf{i} + 2\mathbf{j} - \mathbf{k}$. Find $\mathbf{a} \cdot \mathbf{b}$.
Ans. 5	Ans. -14
7. Let $\mathbf{a} = 3\mathbf{i} + 4\mathbf{j}$, $\mathbf{b} = -\mathbf{i} + 2\mathbf{j}$ and θ is the angle between \mathbf{a} and \mathbf{b} . Find θ .	8. Let $\mathbf{a} = 3\mathbf{i} - 4\mathbf{j} + 12\mathbf{k}$, $\mathbf{b} = 2\mathbf{i} + 2\mathbf{j} - \mathbf{k}$ and θ is the angle between \mathbf{a} and \mathbf{b} . Find θ .
Ans. 63.4°	Ans. 111°
9. Let $\mathbf{a} = 3\mathbf{i} + 4\mathbf{j}$, $\mathbf{b} = -\mathbf{i} + 2\mathbf{j}$. Find the length of projection of \mathbf{b} on \mathbf{a} .	10. Let $\mathbf{a} = 3\mathbf{i} - 4\mathbf{j} + 12\mathbf{k}$, $\mathbf{b} = 2\mathbf{i} + 2\mathbf{j} - \mathbf{k}$. Find the length of projection of \mathbf{b} on \mathbf{a} .
Ans. 1	Ans. $\frac{14}{13}$

<p>11. Let $\mathbf{a} = 3\mathbf{i} + 4\mathbf{j}$, $\mathbf{b} = -\mathbf{i} + 2\mathbf{j}$. Find the projection vector of \mathbf{b} on \mathbf{a}.</p> <p style="text-align: right;">Ans. $\frac{3}{5}\mathbf{i} + \frac{4}{5}\mathbf{j}$</p>	<p>12. Let $\mathbf{a} = 3\mathbf{i} - 4\mathbf{j} + 12\mathbf{k}$, $\mathbf{b} = 2\mathbf{i} + 2\mathbf{j} - \mathbf{k}$. Find the projection vector of \mathbf{a} on \mathbf{b}.</p> <p style="text-align: right;">Ans. $-\frac{28}{9}\mathbf{i} - \frac{28}{9}\mathbf{j} + \frac{14}{9}\mathbf{k}$</p>
<p>13. Let $A = (3, 4)$, $B = (-1, 2)$. Let E be a point on OA such that $BE \perp OA$. Find the vector \overrightarrow{EB}.</p> <p style="text-align: right;">Ans. $-\frac{8}{5}\mathbf{i} + \frac{6}{5}\mathbf{j}$</p>	<p>14. Let $A = (3, -4, 12)$, $B = (2, 2, -1)$. Let F be a point on OB such that $AF \perp OB$. Find the vector \overrightarrow{AF}.</p> <p style="text-align: right;">Ans. $-\frac{55}{9}\mathbf{i} + \frac{8}{9}\mathbf{j} - \frac{94}{9}\mathbf{k}$</p>

15. Determine whether the following points are collinear. If they are not collinear, determine the shortest distance from C to the line determined by AB . Find the point D on the line AB which is nearest to C .
- (a) $A(1, -2, 4)$, $B(5, -8, 6)$, $C(-1, 1, 3)$.
- (b) $A(1, -2, 4)$, $B(5, -8, 6)$, $C(0, 1, 3)$.

(a) A, B, C are collinear.

(b) Not collinear, the shortest distance $= \frac{1}{7}\sqrt{35}$, $-\frac{5}{7}\mathbf{i} + \frac{4}{7}\mathbf{j} + \frac{22}{7}\mathbf{k}$