

Find all integral solutions to the following equation: $\frac{1}{x} - \frac{1}{y} = \frac{1}{2015}$.

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If (x_1, y_1) is a solution, then $\frac{1}{x_1} - \frac{1}{y_1} = \frac{1}{2015}$, then $\frac{1}{-y_1} - \frac{1}{-x_1} = \frac{1}{2015} \Rightarrow (-y_1, -x_1)$ is a solution.

If $x_1 > 0 > y_1$ is a solution, then $\frac{1}{x_1} - \frac{1}{y_1} = \frac{1}{2015}$ is equivalent to $\frac{1}{x_1} + \frac{1}{-y_1} = \frac{1}{2015}$.

Therefore, $(x_1, -y_1)$ is a solution to $\frac{1}{x} + \frac{1}{y} = \frac{1}{2015}$.

First, we find all positive integral solutions (x, y) of $\frac{1}{x} - \frac{1}{y} = \frac{1}{2015}$ such that $y > x$.

$2015 = 5 \times 13 \times 31$, the equation is equivalent to $5 \times 13 \times 31(y - x) = xy$

Case 1 Let $x = a, y = 2015b$, where a and b are positive integers

$$5 \times 13 \times 31(2015b - a) = 5 \times 13 \times 31ab \Rightarrow 2015b - a = ab$$

$$b(2015 - a) + 2015 - a = 5 \times 13 \times 31$$

$$(b + 1)(2015 - a) = 5 \times 403$$

$$b + 1 = 5 \text{ and } 2015 - a = 403$$

$$b = 4, a = 1612$$

$$x = 1612, y = 2015 \times 4 = 8060$$

OR $b + 1 = 13$ and $2015 - a = 155$

$$b = 12, a = 1860$$

$$x = 1860, y = 2015 \times 12 = 24180$$

OR $b + 1 = 31$ and $2015 - a = 65$

$$b = 30, a = 1950$$

$$x = 1950, y = 2015 \times 30 = 60450$$

OR $b + 1 = 65$ and $2015 - a = 31$

$$b = 64, a = 1984$$

$$x = 1984, y = 2015 \times 64 = 128960$$

OR $b + 1 = 155$ and $2015 - a = 13$

$$b = 154, a = 2002$$

$$x = 2002, y = 2015 \times 154 = 310310$$

OR $b + 1 = 403$ and $2015 - a = 5$

$$b = 402, a = 2010$$

$$x = 2010, y = 2015 \times 402 = 810030$$

OR $b + 1 = 2015$ and $2015 - a = 1$

$$b = 2014, a = 2014$$

$$x = 2014, y = 2015 \times 2014 = 4058210$$

Case 2 Let $x = 5a, y = 403b$, where a and b are positive integers

$$5 \times 13 \times 31(403b - 5a) = 5 \times 13 \times 31ab \Rightarrow 403b - 5a = ab$$

$$b(403 - a) + 403 \times 5 - 5a = 5 \times 13 \times 31$$

$$(b + 5)(403 - a) = 13 \times 155$$

$$b + 5 = 13 \text{ and } 403 - a = 155$$

$$b = 8, a = 248$$

$$x = 5 \times 248 = 1240, y = 403 \times 8 = 3224$$

OR $b + 5 = 31$ and $403 - a = 65$

$$b = 26, a = 338$$

$$x = 5 \times 338 = 1690, y = 403 \times 26 = 10478$$

OR $b + 5 = 65$ and $403 - a = 31$

$$b = 60, a = 372$$

$$x = 5 \times 372 = 1860, y = 403 \times 60 = 24180$$

OR $b + 5 = 155$ and $403 - a = 13$

$$\frac{1}{x} - \frac{1}{y} = \frac{1}{2015}$$

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$$b = 150, a = 390$$

$$x = 5 \times 390 = 1950, y = 403 \times 150 = 60450$$

OR $b + 5 = 403$ and $403 - a = 5$

$$b = 398, a = 398$$

$$x = 5 \times 398 = 1990, y = 403 \times 398 = 160394$$

OR $b + 5 = 2015$ and $403 - a = 1$

$$b = 2010, a = 402$$

$$x = 5 \times 402 = 2010, y = 403 \times 2010 = 810030$$

Case 3 Let $x = 13a, y = 155b$, where a and b are positive integers

$$5 \times 13 \times 31(155b - 13a) = 5 \times 13 \times 31ab \Rightarrow 155b - 13a = ab$$

$$b(155 - a) + 13 \times 155 - 13a = 5 \times 13 \times 31$$

$$(b + 13)(155 - a) = 31 \times 65$$

$b + 13 = 31$ and $155 - a = 65$

$$b = 18, a = 90$$

$$x = 13 \times 90 = 1170, y = 155 \times 18 = 2790$$

OR $b + 13 = 65$ and $155 - a = 31$

$$b = 52, a = 124$$

$$x = 13 \times 124 = 1612, y = 155 \times 52 = 8060$$

OR $b + 13 = 155$ and $155 - a = 13$

$$b = 142, a = 142$$

$$x = 13 \times 142 = 1846, y = 155 \times 142 = 22010$$

OR $b + 13 = 403$ and $155 - a = 5$

$$b = 390, a = 150$$

$$x = 13 \times 150 = 1950, y = 155 \times 390 = 60450$$

OR $b + 13 = 2015$ and $155 - a = 1$

$$b = 2002, a = 154$$

$$x = 13 \times 154 = 2002, y = 155 \times 2002 = 310310$$

Case 4 Let $x = 31a, y = 65b$, where a and b are positive integers

$$5 \times 13 \times 31(65b - 31a) = 5 \times 13 \times 31ab \Rightarrow 65b - 31a = ab$$

$$b(65 - a) + 31 \times 65 - 31a = 5 \times 13 \times 31$$

$$(b + 31)(65 - a) = 65 \times 31$$

$b + 31 = 65$ and $65 - a = 31$

$$b = 34, a = 34$$

$$x = 31 \times 34 = 1054, y = 65 \times 34 = 2210$$

OR $b + 31 = 155$ and $65 - a = 13$

$$b = 124, a = 52$$

$$x = 31 \times 52 = 1612, y = 65 \times 124 = 8060$$

OR $b + 31 = 403$ and $65 - a = 5$

$$b = 372, a = 60$$

$$x = 31 \times 60 = 1860, y = 65 \times 372 = 24180$$

OR $b + 31 = 2015$ and $65 - a = 1$

$$b = 1984, a = 64$$

$$x = 31 \times 64 = 1984, y = 65 \times 1984 = 128960$$

Case 5 Let $x = 65a, y = 31b$, where a and b are positive integers

$$5 \times 13 \times 31(31b - 65a) = 5 \times 13 \times 31ab \Rightarrow 31b - 65a = ab$$

$$b(31 - a) + 65 \times 31 - 65a = 5 \times 13 \times 31$$

$$(b + 65)(31 - a) = 155 \times 13$$

$b + 65 = 155$ and $31 - a = 13$

$$b = 90, a = 18$$

$$x = 65 \times 18 = 1170, y = 31 \times 90 = 2790$$

OR $b + 65 = 403$ and $31 - a = 5$

$$\frac{1}{x} - \frac{1}{y} = \frac{1}{2015}$$

$$b = 338, a = 26$$

$$x = 65 \times 26 = 1690, y = 31 \times 338 = 10478$$

OR $b + 65 = 2015$ and $31 - a = 1$

$$b = 1950, a = 30$$

$$x = 65 \times 30 = 1950, y = 31 \times 1950 = 60450$$

Case 6 Let $x = 155a, y = 13b$, where a and b are positive integers

$$5 \times 13 \times 31(13b - 155a) = 5 \times 13 \times 31ab \Rightarrow 13b - 155a = ab$$

$$b(13 - a) + 155 \times 13 - 155a = 5 \times 13 \times 31$$

$$(b + 155)(13 - a) = 403 \times 5$$

$$b + 155 = 403 \text{ and } 13 - a = 5$$

$$b = 248, a = 8$$

$$x = 155 \times 8 = 1240, y = 13 \times 248 = 3224$$

OR $b + 155 = 2015$ and $13 - a = 1$

$$b = 1860, a = 12$$

$$x = 155 \times 12 = 1860, y = 13 \times 1860 = 24180$$

Case 7 Let $x = 403a, y = 5b$, where a and b are positive integers

$$5 \times 13 \times 31(5b - 403a) = 5 \times 13 \times 31ab \Rightarrow 5b - 403a = ab$$

$$b(5 - a) + 403 \times 5 - 403a = 5 \times 13 \times 31$$

$$(b + 403)(5 - a) = 2015 \times 1$$

$$b + 403 = 2015 \text{ and } 5 - a = 1$$

$$b = 1612, a = 4$$

$$x = 403 \times 4 = 1612, y = 5 \times 1612 = 8060$$

Next, we find all positive integral solutions (x, y) of $\frac{1}{x} + \frac{1}{y} = \frac{1}{2015}$. So. $(x, -y)$ is a solution to

$$\frac{1}{x} - \frac{1}{y} = \frac{1}{2015}. \text{ Also, } (y, -x) \text{ is another solution. The equation is equivalent to } 2015(y + x) = xy.$$

Case 8 Let $x = a, y = 2015b$, where a and b are positive integers

$$5 \times 13 \times 31(2015b + a) = 5 \times 13 \times 31ab \Rightarrow 2015b + a = ab$$

$$5 \times 13 \times 31 = 2015 - 2015b + a(b - 1)$$

$$(b - 1)(a - 2015) = 1 \times 2015$$

$$b - 1 = 1 \text{ and } a - 2015 = 2015$$

$$b = 2, a = 4030$$

$$x = 4030, y = 2015 \times 2 = 4030$$

OR $b - 1 = 5$ and $a - 2015 = 403$

$$b = 6, a = 2418$$

$$x = 2418, y = 2015 \times 6 = 12090$$

OR $b - 1 = 13$ and $a - 2015 = 155$

$$b = 14, a = 2170$$

$$x = 2170, y = 2015 \times 14 = 28210$$

OR $b - 1 = 31$ and $a - 2015 = 65$

$$b = 32, a = 2080$$

$$x = 2080, y = 2015 \times 32 = 64480$$

OR $b - 1 = 65$ and $a - 2015 = 31$

$$b = 66, a = 2046$$

$$x = 2046, y = 2015 \times 66 = 132990$$

OR $b - 1 = 155$ and $a - 2015 = 13$

$$b = 156, a = 2028$$

$$x = 2028, y = 2015 \times 156 = 314340$$

OR $b - 1 = 403$ and $a - 2015 = 5$

$$b = 404, a = 2020$$

$$\frac{1}{x} - \frac{1}{y} = \frac{1}{2015}$$

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$$x = 2020, y = 2015 \times 404 = 814060$$

OR $b - 1 = 2015$ and $a - 2015 = 1$

$$b = 2016, a = 2016$$

$$x = 2016, y = 2015 \times 2016 = 4062240$$

Case 9 Let $x = 5a, y = 403b$, where a and b are positive integers

$$5 \times 13 \times 31(403b + 5a) = 5 \times 13 \times 31ab \Rightarrow 403b + 5a = ab$$

$$5 \times 13 \times 31 = 2015 - 403b + a(b - 5)$$

$$(b - 5)(a - 403) = 1 \times 2015$$

$$b - 5 = 1 \text{ and } a - 403 = 2015$$

$$b = 6, a = 2418$$

$$x = 5 \times 2418 = 12090, y = 403 \times 6 = 2418$$

OR $b - 5 = 5$ and $a - 403 = 403$

$$b = 10, a = 806$$

$$x = 5 \times 806 = 4030, y = 403 \times 10 = 4030$$

OR $b - 5 = 13$ and $a - 403 = 155$

$$b = 18, a = 558$$

$$x = 5 \times 558 = 2790, y = 403 \times 18 = 7254$$

OR $b - 5 = 31$ and $a - 403 = 65$

$$b = 36, a = 468$$

$$x = 5 \times 468 = 2340, y = 403 \times 36 = 14508$$

OR $b - 5 = 65$ and $a - 403 = 31$

$$b = 70, a = 434$$

$$x = 5 \times 434 = 2170, y = 403 \times 70 = 28210$$

OR $b - 5 = 155$ and $a - 403 = 13$

$$b = 160, a = 416$$

$$x = 5 \times 416 = 2080, y = 403 \times 160 = 64480$$

OR $b - 5 = 403$ and $a - 403 = 5$

$$b = 408, a = 408$$

$$x = 5 \times 408 = 2040, y = 403 \times 408 = 164424$$

OR $b - 5 = 2015$ and $a - 403 = 1$

$$b = 2020, a = 404$$

$$x = 5 \times 2020 = 2020, y = 403 \times 2020 = 814060$$

Case 10 Let $x = 13a, y = 155b$, where a and b are positive integers

$$5 \times 13 \times 31(155b + 13a) = 5 \times 13 \times 31ab \Rightarrow 155b + 13a = ab$$

$$5 \times 13 \times 31 = 2015 - 155b + a(b - 13)$$

$$(b - 13)(a - 155) = 1 \times 2015$$

$$b - 13 = 1 \text{ and } a - 155 = 2015$$

$$b = 14, a = 2170$$

$$x = 13 \times 2170 = 28210, y = 155 \times 14 = 2170$$

OR $b - 13 = 5$ and $a - 155 = 403$

$$b = 18, a = 558$$

$$x = 13 \times 558 = 7254, y = 155 \times 18 = 2790$$

OR $b - 13 = 13$ and $a - 155 = 155$

$$b = 26, a = 310$$

$$x = 13 \times 310 = 4030, y = 155 \times 26 = 4030$$

OR $b - 13 = 31$ and $a - 155 = 65$

$$b = 44, a = 220$$

$$x = 13 \times 220 = 2860, y = 155 \times 44 = 6820$$

OR $b - 13 = 65$ and $a - 155 = 31$

$$b = 78, a = 186$$

$$x = 13 \times 186 = 2418, y = 155 \times 78 = 12090$$

$$\frac{1}{x} - \frac{1}{y} = \frac{1}{2015}$$

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OR $b - 13 = 155$ and $a - 155 = 13$

$$b = 168, a = 168$$

$$x = 13 \times 168 = 2184, y = 155 \times 168 = 26040$$

OR $b - 13 = 403$ and $a - 155 = 5$

$$b = 416, a = 160$$

$$x = 13 \times 160 = 2080, y = 155 \times 416 = 64480$$

OR $b - 13 = 2015$ and $a - 155 = 1$

$$b = 2028, a = 156$$

$$x = 13 \times 156 = 2028, y = 155 \times 2028 = 314340$$

Case 11 Let $x = 31a, y = 65b$, where a and b are positive integers

$$5 \times 13 \times 31(65b + 31a) = 5 \times 13 \times 31ab \Rightarrow 65b + 31a = ab$$

$$5 \times 13 \times 31 = 2015 - 65b + a(b - 31)$$

$$(b - 31)(a - 65) = 1 \times 2015$$

$b - 31 = 1$ and $a - 65 = 2015$

$$b = 32, a = 2080$$

$$x = 31 \times 2080 = 64480, y = 65 \times 32 = 2080$$

OR $b - 31 = 5$ and $a - 65 = 403$

$$b = 36, a = 468$$

$$x = 31 \times 468 = 14508, y = 65 \times 36 = 2340$$

OR $b - 31 = 13$ and $a - 65 = 155$

$$b = 44, a = 220$$

$$x = 31 \times 220 = 6820, y = 65 \times 44 = 2860$$

OR $b - 31 = 31$ and $a - 65 = 65$

$$b = 62, a = 130$$

$$x = 31 \times 130 = 4030, y = 65 \times 62 = 4030$$

OR $b - 31 = 65$ and $a - 65 = 31$

$$b = 96, a = 96$$

$$x = 31 \times 96 = 2976, y = 65 \times 96 = 6240$$

OR $b - 31 = 155$ and $a - 65 = 13$

$$b = 186, a = 78$$

$$x = 31 \times 78 = 2418, y = 65 \times 186 = 12090$$

OR $b - 31 = 403$ and $a - 65 = 5$

$$b = 434, a = 70$$

$$x = 31 \times 70 = 2170, y = 65 \times 434 = 28210$$

OR $b - 31 = 2015$ and $a - 65 = 1$

$$b = 2046, a = 66$$

$$x = 31 \times 66 = 2046, y = 65 \times 2046 = 132990$$

Case 12 Let $x = 65a, y = 31b$, where a and b are positive integers

$$5 \times 13 \times 31(31b + 65a) = 5 \times 13 \times 31ab \Rightarrow 31b + 65a = ab$$

$$5 \times 13 \times 31 = 2015 - 31b + a(b - 65)$$

$$(b - 65)(a - 31) = 1 \times 2015$$

$b - 65 = 1$ and $a - 31 = 2015$

$$b = 66, a = 2046$$

$$x = 65 \times 2046 = 132990, y = 31 \times 66 = 2046$$

OR $b - 65 = 5$ and $a - 31 = 403$

$$b = 70, a = 434$$

$$x = 65 \times 434 = 28210, y = 31 \times 70 = 2170$$

OR $b - 65 = 13$ and $a - 31 = 155$

$$b = 78, a = 186$$

$$x = 65 \times 186 = 12090, y = 31 \times 78 = 2418$$

OR $b - 65 = 31$ and $a - 31 = 65$

$$\frac{1}{x} - \frac{1}{y} = \frac{1}{2015}$$

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$$b = 96, a = 96$$

$$x = 65 \times 96 = 6240, y = 31 \times 96 = 2976$$

OR $b - 65 = 65$ and $a - 31 = 31$

$$b = 130, a = 62$$

$$x = 65 \times 62 = 4030, y = 31 \times 130 = 4030$$

OR $b - 65 = 155$ and $a - 31 = 13$

$$b = 220, a = 44$$

$$x = 65 \times 44 = 2860, y = 31 \times 220 = 6820$$

OR $b - 65 = 403$ and $a - 31 = 5$

$$b = 468, a = 36$$

$$x = 65 \times 36 = 2340, y = 31 \times 468 = 14508$$

OR $b - 65 = 2015$ and $a - 31 = 1$

$$b = 2080, a = 32$$

$$x = 65 \times 32 = 2080, y = 31 \times 2080 = 64480$$

Case 13 Let $x = 155a, y = 13b$, where a and b are positive integers

$$5 \times 13 \times 31(13b + 155a) = 5 \times 13 \times 31ab \Rightarrow 13b + 155a = ab$$

$$5 \times 13 \times 31 = 2015 - 13b + a(b - 155)$$

$$(b - 155)(a - 13) = 1 \times 2015$$

$b - 155 = 1$ and $a - 13 = 2015$

$$b = 156, a = 2028$$

$$x = 155 \times 2028 = 314340, y = 13 \times 156 = 2028$$

OR $b - 155 = 5$ and $a - 13 = 403$

$$b = 160, a = 416$$

$$x = 155 \times 416 = 64480, y = 13 \times 160 = 2080$$

OR $b - 155 = 13$ and $a - 13 = 155$

$$b = 168, a = 168$$

$$x = 155 \times 168 = 26040, y = 13 \times 168 = 2184$$

OR $b - 155 = 31$ and $a - 13 = 65$

$$b = 186, a = 78$$

$$x = 155 \times 78 = 12090, y = 13 \times 186 = 2418$$

OR $b - 155 = 65$ and $a - 13 = 31$

$$b = 220, a = 44$$

$$x = 155 \times 44 = 6820, y = 13 \times 220 = 2860$$

OR $b - 155 = 155$ and $a - 13 = 13$

$$b = 310, a = 26$$

$$x = 155 \times 26 = 4030, y = 13 \times 310 = 4030$$

OR $b - 155 = 403$ and $a - 13 = 5$

$$b = 558, a = 18$$

$$x = 155 \times 18 = 2790, y = 13 \times 558 = 7254$$

OR $b - 155 = 2015$ and $a - 13 = 1$

$$b = 2170, a = 14$$

$$x = 155 \times 14 = 2170, y = 13 \times 2170 = 28210$$

Case 14 Let $x = 403a, y = 5b$, where a and b are positive integers

$$5 \times 13 \times 31(5b + 403a) = 5 \times 13 \times 31ab \Rightarrow 5b + 403a = ab$$

$$5 \times 13 \times 31 = 2015 - 5b + a(b - 403)$$

$$(b - 403)(a - 5) = 1 \times 2015$$

$b - 403 = 1$ and $a - 5 = 2015$

$$b = 404, a = 2020$$

$$x = 403 \times 2020 = 814060, y = 5 \times 404 = 2020$$

OR $b - 403 = 5$ and $a - 5 = 403$

$$b = 408, a = 408$$

$$\frac{1}{x} - \frac{1}{y} = \frac{1}{2015}$$

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$$x = 403 \times 408 = 164424, y = 5 \times 408 = 2040$$

OR $b - 403 = 13$ and $a - 5 = 155$

$$b = 416, a = 160$$

$$x = 403 \times 160 = 64480, y = 5 \times 416 = 2080$$

OR $b - 403 = 31$ and $a - 5 = 65$

$$b = 434, a = 70$$

$$x = 403 \times 70 = 28210, y = 5 \times 434 = 2170$$

OR $b - 403 = 65$ and $a - 5 = 31$

$$b = 468, a = 36$$

$$x = 403 \times 36 = 14508, y = 5 \times 468 = 2340$$

OR $b - 403 = 155$ and $a - 5 = 13$

$$b = 558, a = 18$$

$$x = 403 \times 18 = 7254, y = 5 \times 558 = 2790$$

OR $b - 403 = 403$ and $a - 5 = 5$

$$b = 806, a = 10$$

$$x = 403 \times 10 = 4030, y = 5 \times 806 = 4030$$

OR $b - 403 = 2015$ and $a - 5 = 1$

$$b = 2418, a = 6$$

$$x = 403 \times 6 = 2418, y = 5 \times 2418 = 12090$$

Case 15 Let $x = 2015a, y = b$, where a and b are positive integers

$$5 \times 13 \times 31(b + 2015a) = 5 \times 13 \times 31ab \Rightarrow b + 2015a = ab$$

$$5 \times 13 \times 31 = 2015 - b + a(b - 2015)$$

$$(b - 2015)(a - 1) = 1 \times 2015$$

$$b - 2015 = 1 \text{ and } a - 1 = 2015$$

$$b = 2016, a = 2016$$

$$x = 2015 \times 2016 = 4062240, y = 2016$$

OR $b - 2015 = 5$ and $a - 1 = 403$

$$b = 2020, a = 404$$

$$x = 2015 \times 404 = 814060, y = 2020$$

OR $b - 2015 = 13$ and $a - 1 = 155$

$$b = 2028, a = 156$$

$$x = 2015 \times 156 = 314340, y = 2028$$

OR $b - 2015 = 31$ and $a - 1 = 65$

$$b = 2046, a = 66$$

$$x = 2015 \times 66 = 132990, y = 2046$$

OR $b - 2015 = 65$ and $a - 1 = 31$

$$b = 2080, a = 32$$

$$x = 2015 \times 32 = 64480, y = 2080$$

OR $b - 2015 = 155$ and $a - 1 = 13$

$$b = 2170, a = 14$$

$$x = 2015 \times 14 = 28210, y = 2170$$

OR $b - 2015 = 403$ and $a - 1 = 5$

$$b = 2418, a = 6$$

$$x = 2015 \times 6 = 12090, y = 2418$$

OR $b - 2015 = 2015$ and $a - 1 = 1$

$$b = 4030, a = 2$$

$$x = 2015 \times 2 = 4030, y = 4030$$

$$\frac{1}{x} - \frac{1}{y} = \frac{1}{2015}$$

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∴ The solutions are $(x, y) = (1054, 2210), (1170, 2790), (1240, 3224), (1612, 8060), (1690, 10478), (1846, 22010), (1860, 24180), (1950, 60450), (1984, 128960), (1990, 160394), (2002, 310310), (2010, 810030), (2014, 4058210).$

OR $(-2210, -1054), (-2790, -1170), (-3224, -1240), (-8060, -1612), (-10478, -1690), (-22010, -1846), (-24180, -1860), (-60450, -1950), (-128960, -1984), (-160394, -1990), (-310310, -2002), (-810030, -2010), (-4058210, -2014).$

OR

$(2016, -4062240), (2020, -814060), (2040, -164424), (2046, -132990), (2028, -314340), (2080, -64480), (2170, -28210), (2184, -26040), (2340, -14508), (2418, -12090), (2790, -7254), (2860, -6820), (2976, -6240), (4030, -4030), (6240, -2976), (6820, -2860)$

OR

$(7254, -2790), (12090, -2418), (14508, -2340), (26040, -2184), (28210, -2170), (64480, -2080), (132990, -2046), (164424, -2040), (314340, -2028), (814060, -2020), (4062240, -2016).$