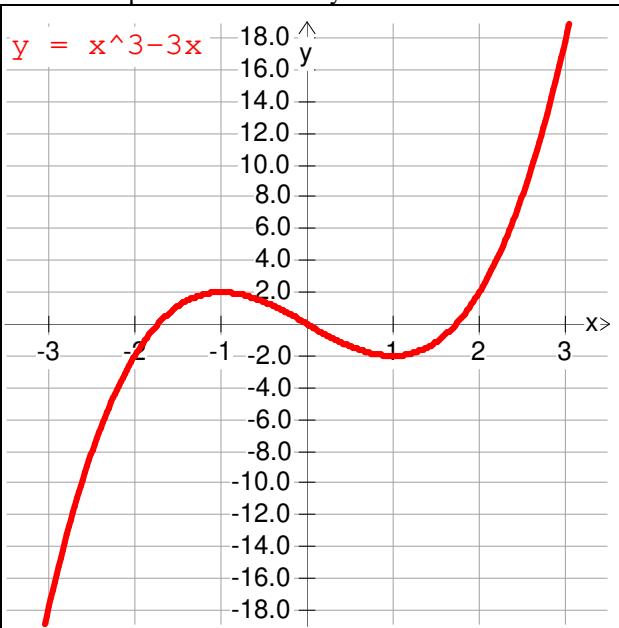
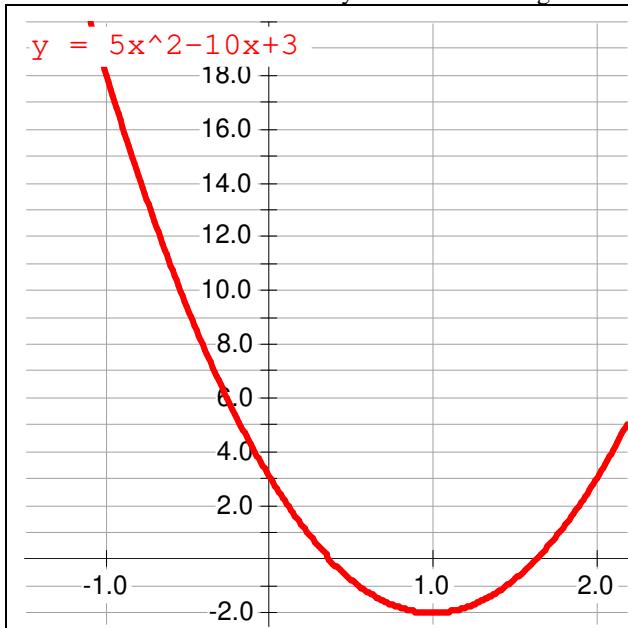


## Maximum, minimum and turning points

Created by Mr. Francis Hung on 20220211. Last updated: 12 February 2022.



Given  $f(x) = 5x^2 - 10x + 3$ .

For  $-1 \leq x \leq 2$ , the local minimum is \_\_\_\_\_.

The local maximum are \_\_\_\_\_.

The absolute minimum is \_\_\_\_\_.

The absolute maximum is \_\_\_\_\_.

The turning point is ( , ).

Given  $f(x) = x^3 - 3x$ .

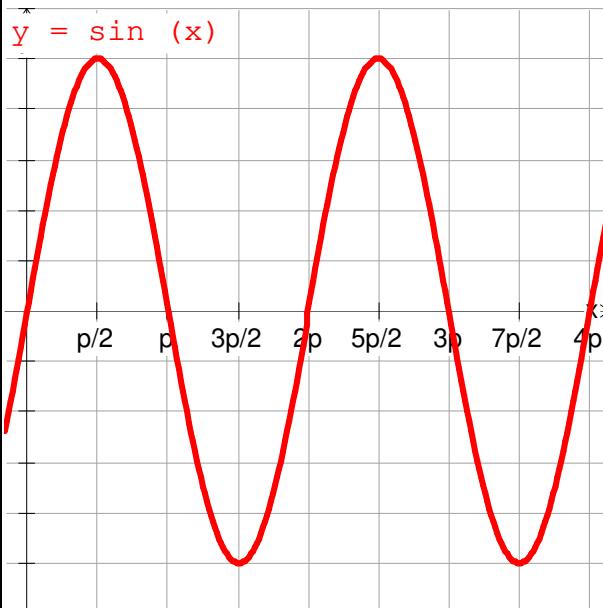
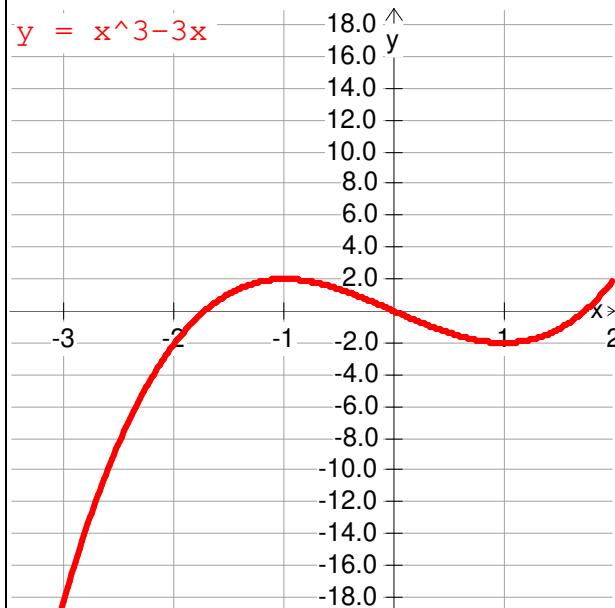
For  $-3 \leq x \leq 3$ , the local minimum are \_\_\_\_\_.

The local maximum are \_\_\_\_\_.

The absolute minimum is \_\_\_\_\_.

The absolute maximum is \_\_\_\_\_.

The turning points are ( , ), ( , ).



Given  $f(x) = x^3 - 3x$ .

For  $-3 \leq x \leq \sqrt{3}$ , the local minimum are \_\_\_\_\_.

The local maximum are \_\_\_\_\_.

The absolute minimum is \_\_\_\_\_.

The absolute maximum is \_\_\_\_\_.

The turning points are ( , ), ( , ).

Given  $f(x) = \sin x$ .

For  $0 \leq x \leq 4\pi$ , the local minimum are \_\_\_\_\_.

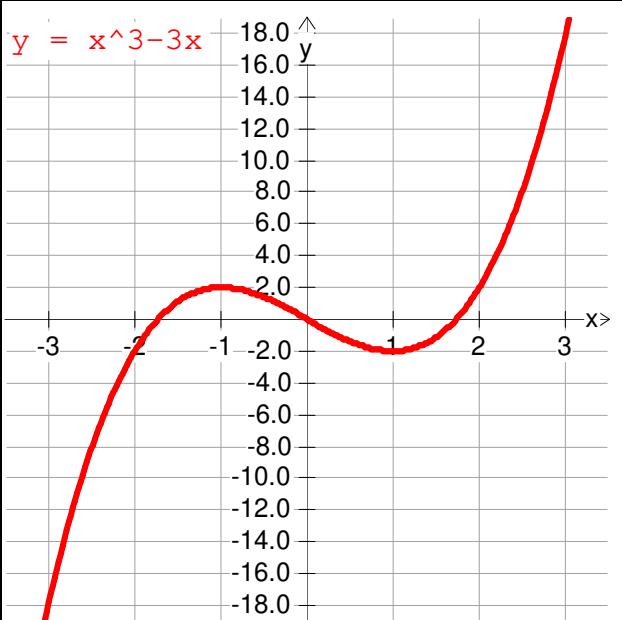
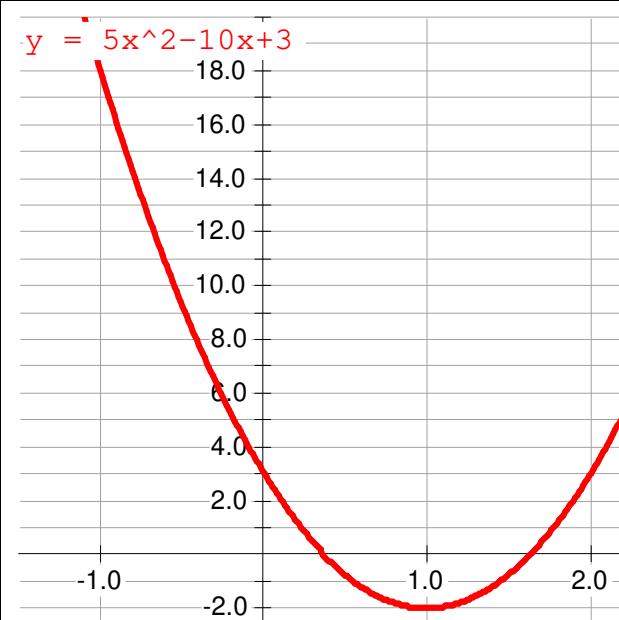
The local maximum are \_\_\_\_\_.

The absolute minimum is \_\_\_\_\_.

The absolute maximum is \_\_\_\_\_.

The turning points are ( , ), ( , ), ( , ) or ( , ).

The absolute maximum and the absolute minimum occur either at \_\_\_\_\_ or \_\_\_\_\_.



Given  $f(x) = 5x^2 - 10x + 3$ .

For  $-1 \leq x \leq 2$ , the local minimum is  $-2$ .

The local maximum are  $3$  and  $18$ .

The absolute minimum is  $-2$ .

The absolute maximum is  $18$ .

The turning point is  $(1, -2)$ .

Given  $f(x) = x^3 - 3x$

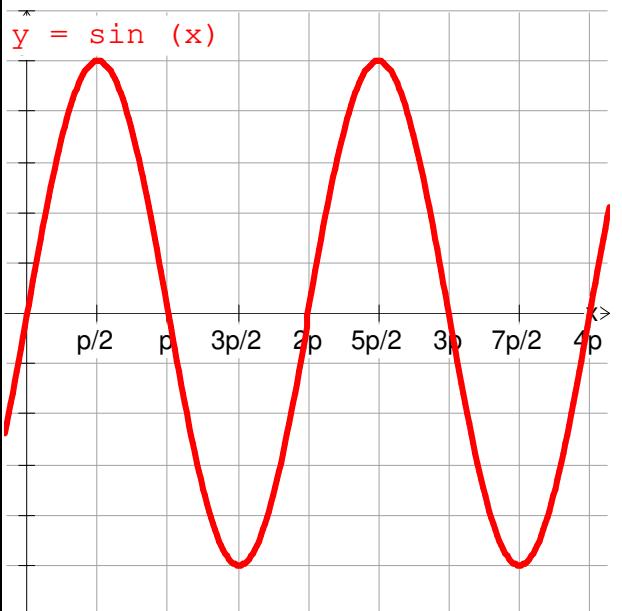
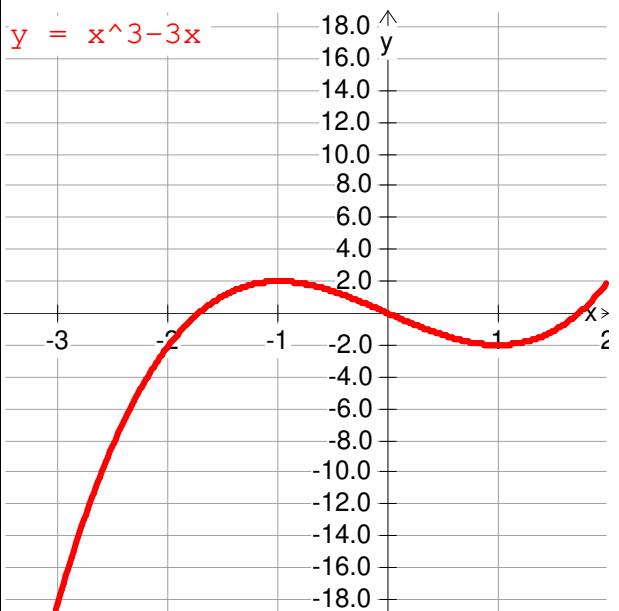
For  $-3 \leq x \leq 3$ , the local minimum are  $-18$  and  $-2$ .

The local maximum are  $2$  and  $18$ .

The absolute minimum is  $-18$ .

The absolute maximum is  $18$ .

The turning points are  $(-1, 2)$  and  $(1, -2)$ .



Given  $f(x) = x^3 - 3x$ .

For  $-3 \leq x \leq \sqrt{3}$ , the local minimum are  $-18, -2$ .

The local maximum are  $2$  and  $0$ .

The absolute minimum is  $-18$ .

The absolute maximum is  $2$ .

The turning points are  $(-1, 2)$  and  $(1, -2)$ .

Given  $f(x) = \sin x$ .

For  $0 \leq x \leq 4\pi$ , the local minimum are  $0$  and  $-1$ .

The local maximum are  $0$  and  $1$ .

The absolute minimum is  $-1$ .

The absolute maximum is  $1$ .

The turning points are  $(\frac{\pi}{2}, 1), (\frac{3\pi}{2}, -1), (\frac{5\pi}{2}, 1), (\frac{7\pi}{2}, -1)$ .

The absolute maximum and the absolute minimum occur either at turning points or boundaries (i.e. end points).